

Fig. 11.7 The strain and stress block at failure of a prestressed masonry beam.

The ultimate strain ε_{su} in prestressing steel consists of strain due to prestress and applied load, hence

$$\varepsilon_{\rm su} = \varepsilon_{\rm sa} + \varepsilon_{\rm se} \tag{11.19}$$

where ε_{sa} is due to applied load and ε_{se} is due to effective prestress after losses. From Fig. 11.7(b) it can be seen that strain due to the applied load is equal to

$$\varepsilon_{\rm sa} = \varepsilon_{\rm ma} + \varepsilon_{\rm me}$$

where

$$\varepsilon_{\rm me} = {{\rm prestressing stress at tendon level}\over E_{\rm m}}$$
 (11.20)

Assuming full bond exists between the steel, grout and masonry at failure, then the strain in steel may be given by

$$\varepsilon_{\rm sa} = \varepsilon_{\rm m} \left(\frac{d - d_{\rm c}}{d_{\rm c}} \right) + \varepsilon_{\rm me} \tag{11.21}$$

Substituting the value of ε_{sa} from equation (11.21) into equation (11.19), we get

$$\epsilon_{su} = \epsilon_m \left(\frac{d - d_c}{d_c} \right) + \epsilon_{me} + \epsilon_{se}$$

or

$$d_{c} = \frac{\varepsilon_{m}}{\varepsilon_{su} + \varepsilon_{m} - \varepsilon_{me} - \varepsilon_{se}} d \qquad (11.22)$$

Combining equations (11.18) and (11.22) gives

$$f_{\rm su} = \frac{\lambda_1 f_{\rm m} b d}{A_{\rm ps}} \frac{\varepsilon_{\rm m}}{\varepsilon_{\rm su} + \varepsilon_{\rm m} - \varepsilon_{\rm me} - \varepsilon_{\rm se}}$$
$$= \frac{\lambda_1 f_{\rm m}}{\rho} \frac{\varepsilon_{\rm m}}{\varepsilon_{\rm su} + \varepsilon_{\rm m} - \varepsilon_{\rm me} - \varepsilon_{\rm se}}$$
(11.23)

At the ultimate limit state, the values of f_{su} and ε_{su} must satisfy equation (11.23) and also define a point on the stress-strain curve for the steel (see Fig. 2.7). Having found f_{su} and the tendon strain ε_{su} , the depth of the neutral axis d_c can be obtained from equation (11.22). The ultimate moment of resistance is then

$$M_{\rm u} = A_{\rm su} f_{\rm su} (d - \lambda_2 d_c)$$

= $A_{\rm su} f_{\rm su} \left(1 - \rho \frac{\lambda_2 f_{\rm su}}{\lambda_1 f_{\rm m}} \right) d$ (11.24)

Generally, an idealized stress block is used for design purposes. Figure 11.7(d) shows the rectangular stress block suggested in the British Code of Practice for prestressed masonry. The values of λ_1 and λ_2 corresponding to this stress block are 1 and 0.5.

The materials partial safety factors are γ_{mm} for masonry and γ_{ms} for steel. The general flexural theory given in this section can easily be modified to take account of these.

Example 3

A bonded post-tensioned masonry beam of rectangular cross-section $210 \times 365 \text{ mm}$ as shown in Fig. 11.8 has been prestressed to effective stress of 900 N/mm² by four 10.9 mm diameter stabilized strands of characteristic strength of 1700 N/mm². The area of steel provided is 288mm². The initial modulus of elasticity of the steel is 195 kN/mm² and the stress-strain relationship is given in Fig. 2.7. The masonry in $1:\frac{1}{4}:3$ mortar has a characteristic strength parallel to the bed joint of 21N/mm² and modulus of elasticity 15.3kN/mm².

Using the simplified stress block of BS 5628: Part 2, calculate the ultimate moment of resistance of the beam.

Solution We have

area
$$A = 210 \times 365 = 76\ 650\ \text{mm}^2$$

 $I = bd^3/12 = 210 \times (365)^3/12 = 8.5 \times 10^8\ \text{mm}^4$
 $P_e = 900 \times 288 = 259.2 \times 10^3\ \text{N}$